

# Design and Simulation of Miniaturized Minkowski Fractal Aperture-Coupled Antenna for 5.8 GHz RFID Applications

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## ABSTRACT

A miniaturized 3rd-order Minkowski fractal aperture-coupled antenna is designed for 5.8 GHz RFID applications using particle swarm optimization (PSO) technique. The PSO technique runs on MATLAB environment and synchronously coupled with an electromagnetic simulator (CST Microwave Studio) to estimate the radiation pattern parameters at each optimization iteration. Two objective functions are used to optimize the geometry of the antenna: return loss and the relative antenna size with respect to the reference (non-fractal) antenna. The simulated results show that the optimized fractal antenna has less than -37 dB return loss, more than 65% reduction in patch area and, more than 4 dB gains.

**Keywords:** Aperture-coupled antenna, Minkowski fractal antenna, Particle swarm optimization, RFID.

## 1. INTRODUCTION

Radio frequency identification (RFID) has excelled in automatic identification, bioengineering applications and data collection industry through its speed, agility, and endurance [1]. Recently, the operating frequency of RFID systems moves towards higher frequencies such as ISM band (5.8 GHz) to achieve higher identification range with higher data transfer rate [2]. This motivates researchers to apply micro strip antenna technology for RFID systems to gain the advantages of low profile, light weight, small volume, and mass production [3, 4]. For micro strip patch antennas, aperture coupling is preferred to other feeding mechanisms as it offers greater design flexibility [5, 6]. Aperture coupling has considerable advantage as a feeding mechanism particularly in fractal designs where identifying a suitable feed position on such complex geometrical shapes is particularly difficult [7].

Miniaturization of micro strip patch antenna has been typically accomplished by a suitable loading. One common technique in loading is to modify basic patch shapes. Applying fractals to antenna elements allows for smaller size, multiband, and broad-band properties. This is the cause of widespread research on fractal antennas in recent years [8-10]. Fractal geometries have self-similarity and space-filling nature when applied to antenna design [11-13]; and they can realize multi-frequency and size-reducing features. Several fractal geometries have been explored for antennas with special characteristics, such as the Sierpinski monopole [14], Koch curves [15] and the tree monopole [16]. These fractal geometries verify that the fractal antenna has size-reducing features within limited space.

The design of RFID antenna is still a challenge for miniaturization system due to the limited available area. This paper presents feasibility study to design miniaturized aperture-coupled micro strip antenna for 5.8 GHz RFID applications. The antenna miniaturization is achieved through two phases. The first phase applies

fractal geometry while the second phase adopts particle swarm optimization (PSO) technique to get further area reduction. The CST Microwave Studio is used during the optimization process as an electromagnetic (EM) simulator to extract the antenna performance parameters that enter the objective function.

## 2. DESIGN METHODOLOGY

Particle swarm optimization algorithm has been tested by different research groups to different benchmark functions and results show that it is an excellent global optimizer that can be used for different electromagnetic problems especially antenna miniaturization [17, 18]. To calculate the antenna fitness function associated with the PSO algorithm, a comprehensive numerical modeling must be carried out to simulate the EM performance of the antenna at each iteration of optimization. The EM model should be very efficient in both speed of computation and accuracy since the geometry of the fractal antenna is relatively more complicated than the conventional counterpart and the dimensions of some structure parameters are much smaller than the operating wavelength. The required EM model features are recovered in this paper by using a commercial EM simulator namely CST MWS. This simulator uses finite integration time domain (FITD) method to assign the EM properties of antennas and has been proven in the literature as a powerful and very accurate tool for this purpose.

In this work, the fractal RFID antenna is optimized using PSO technique while the FITD method is used in parallel with it to compute the EM part of the fitness function (see Fig. 1). The PSO technique runs under MATLAB environment and the FITD method is offered by CST MWS software package. For each generation of the PSO algorithm, the antenna geometrical parameters are updated and mapped to CST MWS to simulate the EM properties of the antenna. According to the EM simulator

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results that mapped back to MATLAB environment, the fitness function is evaluated by the PSO kernel.

Where

$$obj_{S_{11}} = (S_{11 \text{ at } f_r} - (S_{11})_{th}) \cdot u(S_{11 \text{ at } f_r} - (S_{11})_{th}) \quad (3b)$$

and

$$obj_{Area} = \left( \frac{A_F}{A_R} - 1 \right) \quad (3c)$$

where  $obj_{S_{11}}$  and  $obj_{Area}$  denote the return loss and area objective functions, respectively.

The objective function  $obj_{S_{11}}$  represents the amount of matching at the desired frequency  $f_r$  and its value between "0" and  $-(S_{11})_{th}$ . Its zero value denotes that the goal is achieved, that is to say a return loss of at least  $(S_{11})_{th}$  at the desired frequency  $f_r$  is satisfied. The objective function  $obj_{Area}$  is used to achieve a minimum area from the optimization process. The range of  $obj_{Area}$  is between (0, -1); it is zero if the area of the fractal antenna is equal to the area of the *reference* counterpart, and to "-1" when the area of the fractal antenna is zero (not physically allowed). Thus the value of the total fitness function "Fit" which is considered as multiobjective optimization problem ranges between minimum values of "-1" to a maximum value of  $-(S_{11})_{th}$ .

The antenna miniaturization methodology for the fractal micro strip antenna is performed using the following three steps

- Design a conventional (non-fractal) aperture-coupled micro strip antenna using CST MWS. The dimensions of the structure parameters are tuned to achieve the design requirements ( $S_{11} \leq (S_{11})_{th}$ ) at the desired resonance frequency  $f_r$ . This antenna will be considered as a reference antenna (RA) for the design of the 3rd-order fractal antenna and its area is denoted by  $A_R$ .
- Introduce the 3rd-order Minkowski geometry on the RA (see Fig. 2).
- The 3rd-order fractal antenna (MFA3) is optimized with respect to the reference antenna according to the fitness function defined in eqn. (1).

### 3. DESIGN OF MINIATURIZED MINKOWSKI FRACTAL APERTURE-COUPLED ANTENNA

#### 3.1. Reference Antenna

An aperture coupled micro strip patch structure having square ground ( $L_g = W_g = 20 \text{ mm}$ ) is used as the reference (RA) (see Fig. 3). For the RA, the basic formulas for determining the length  $L_p$  and width  $W_p$  of the microstrip patch are [19]

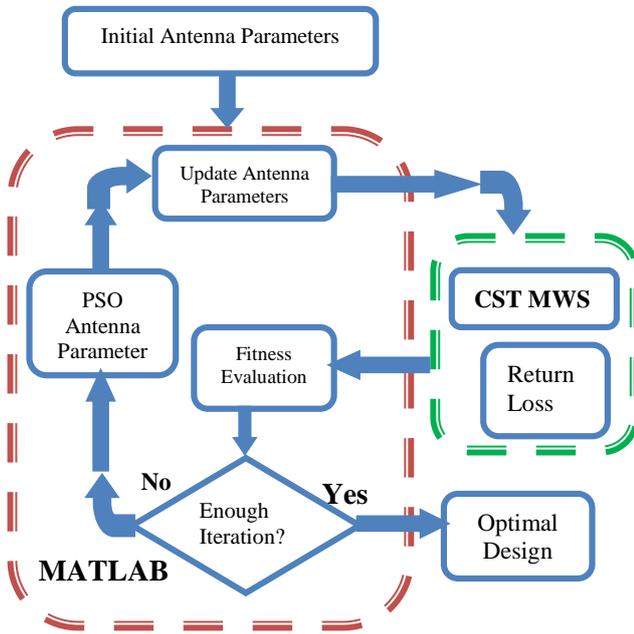


Fig 1: Data flow of the PSO/FITD algorithm.

The goal for the electromagnetic miniaturization design considered here is to minimize the size of the fractal antenna by altering the geometrical parameters within allowed prescribed ranges while keeping the return loss below a desired threshold value  $(S_{11})_{th}$  at the required resonance frequency  $f_r$ . A suitable optimization model is Minimize the fitness function

$$Fit(x) = (S_{11 \text{ at } f_r} - (S_{11})_{th}) \cdot u(S_{11 \text{ at } f_r} - (S_{11})_{th}) + \left( \frac{A_F}{A_R} - 1 \right) \quad (1)$$

Subject to  $A_F < A_R$   
and the constraints:  $x_i^l \leq x_i \leq x_i^u$ ,  
 $i = 1, 2, \dots, N$

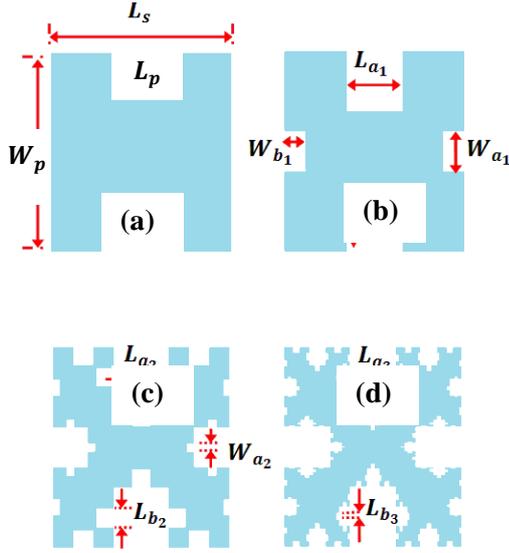
where

$$S_{11 \text{ at } f_r} = 20 \log \left| \frac{Z_{in \text{ at } f_r} - Z_o}{Z_{in \text{ at } f_r} + Z_o} \right| \text{ (dB)} \quad (2)$$

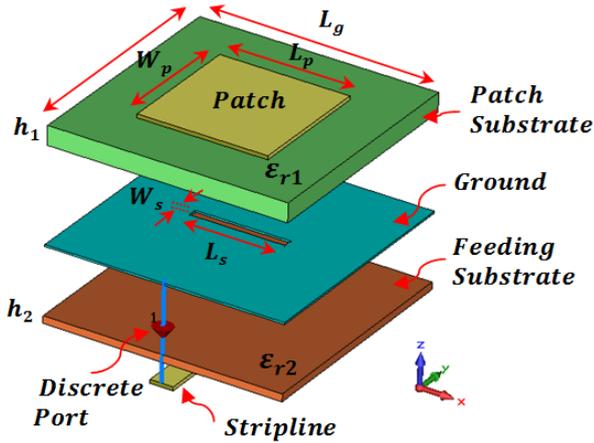
In eqn. (1),  $u$  refers to the Heaviside step function while  $A_F$  and  $A_R$  denote, respectively, the area of the fractal and reference antennas. In eqn. (2),  $S_{11 \text{ at } f_r}$  and  $Z_{in \text{ at } f_r}$  refer, respectively, to the return loss and the input impedance of the antenna at the resonance frequency  $f_r$ , and  $Z_o$  is the characteristic impedance ( $Z_o = 50\Omega$ ).

Note that the optimization fitness function eqn. (1) consists of two objective functions which are related to antenna return loss  $S_{11}$  and antenna area.

$$Fit = obj_{S_{11}} + obj_{Area} \quad (3a)$$



**Fig 2:** Scheme of the Minkowski fractal geometry (a) zero order (b) 1st order (c) 2nd order (d) 3rd order.



**Fig 3:** Aperture coupled-patch antenna.

$$W_p = \frac{c}{2f_r} \sqrt{\frac{2}{\epsilon_r + 1}} \quad (4)$$

$$\epsilon_{eff} = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \left( \frac{1}{\sqrt{1 + 12h_1/W_p}} \right) \quad (5)$$

$$\Delta L_p = 0.412 h_1 \frac{(\epsilon_{eff} + 0.300) \left[ \frac{W_p}{h_1} + 0.264 \right]}{(\epsilon_{eff} - 0.258) \left[ \frac{W_p}{h_1} + 0.813 \right]} \quad (6)$$

$$L_p = \frac{c}{2f_r \sqrt{\epsilon_{eff}}} - 2\Delta L \quad (7)$$

where  $W_p$  is the patch width,  $L_p$  is the patch length,  $\Delta L_p$  is the patch length reduced from the patch antenna to reduce fringing effects,  $\epsilon_r$  is the dielectric constant,  $c$  is the speed of wave in free space, and  $\epsilon_{eff}$  is the effective dielectric constant. Using eqns. 4-7, the patch antenna is designed using Rogers 5880 substrate for patch and feed with dielectric constant  $\epsilon_r = 2.2$  and loss tangent of  $0.0009$ . Table 1 illustrates the designed parameters of the reference aperture-coupled antenna at 5.8 GHz.

**Table 1:** Designed reference antenna geometrical parameters to achieve  $f_r = 5.8 \text{ GHz}$ .

| Parameter                | Symbol   | Value (mm) |
|--------------------------|----------|------------|
| Ground length            | $L_g$    | 20.00      |
| Ground width             | $W_g$    | 20.00      |
| Patch length             | $L_p$    | 14.50      |
| Patch width              | $W_p$    | 14.50      |
| Stripline length         | $L_{st}$ | 15.30      |
| Ground slot length       | $L_s$    | 7.00       |
| Ground slot width        | $W_s$    | 1.11       |
| Patch substrate height   | $h_1$    | 1.60       |
| Feeding substrate height | $h_2$    | 0.80       |

### 3.2 Third-order Minkowski Fractal Antenna

In this subsection, a 3rd-order Minkowski fractal aperture-coupled antenna (MFA3) is optimized at **5.8 GHz** resonance frequency after miniaturizing the patch for fixed ground plane of size (**20 mm × 20 mm**), see Fig. 2. Its shown from this figure that eight geometrical parameters enters the optimization process, five describing the patch side (patch length  $L_p$  and fractal scales parameters  $K_{L_a}$ ,  $K_{L_b}$ ,  $K_{W_a}$ , and  $K_{W_b}$ ), two for the ground side (aperture slot length  $L_s$  and width  $W_s$ ). The remain parameter is strip line length  $L_{st}$  related to the feeding side. In the optimization process, all the eight geometrical parameters are scaled version from ground length  $L_g$  ( $W_g = L_g$ ) as

$$L_p = W_p = K_{L_p} \times L_g \quad (8a)$$

$$L_s = K_{L_s} \times L_p = K_{L_p} \times K_{L_s} \times L_g \quad (8b)$$

$$W_s = K_{W_s} \times L_p = K_{W_s} \times K_{L_p} \times L_g \quad (8c)$$

$$\begin{aligned} L_{st} &= K_{L_{st}} \times L_p + 0.5L_g \\ &= K_{L_{st}} \times K_{L_p} \times L_g + 0.5L_g \end{aligned} \quad (8d)$$

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The fractal scaling factors are introduced here for any fractal order. For 3rd-order geometry, these four scaling factors are  $K_{L_a}$ ,  $K_{L_b}$ ,  $K_{W_a}$ , and  $K_{W_b}$  defined as follows

$$L_a^{(n)} = (K_{L_a})^n \times L_p \tag{9a}$$

$$L_b^{(n)} = (K_{L_b})^n \times W_p \tag{9b}$$

$$W_a^{(n)} = (K_{W_a})^n \times W_p \tag{9c}$$

$$W_b^{(n)} = (K_{W_b})^n \times L_p \tag{9d}$$

$$n = 1, 2, \dots, n_{des}$$

where

$$L_{a1} = L_a^{(1)}, L_{a2} = L_a^{(2)}, L_{a3} = L_a^{(3)} \tag{10a}$$

$$L_{b1} = L_b^{(1)}, L_{b2} = L_b^{(2)}, L_{b3} = L_b^{(3)} \tag{10b}$$

$$W_{a1} = W_a^{(1)}, W_{a2} = W_a^{(2)}, W_{a3} = W_a^{(3)} \tag{10c}$$

$$W_{b1} = W_b^{(1)}, W_{b2} = W_b^{(2)}, W_{b3} = W_b^{(3)} \tag{10d}$$

The optimization model of eqn. (1) is applied here in order to miniaturize patch size while keeping the ground size fixed as (20mm × 20mm).

The constraints used in the optimization process for the geometrical parameters are illustrated in Table 2

**Table 2:** Design parameter constraints used for optimizing MFA3.

| Parameter                    | Symbol       | Ranges      |
|------------------------------|--------------|-------------|
| Patch length scale           | $K_{L_p}$    | 0.10 ~ 0.72 |
| Ground slot length scale     | $K_{L_s}$    | 0.25 ~ 1.25 |
| Ground slot width scale      | $K_{W_s}$    | 0.05 ~ 0.25 |
| Stripline length scale       | $K_{L_{st}}$ | 0.00 ~ 0.6  |
| Fractal patch length scale 1 | $K_{L_a}$    | 0.10 ~ 0.33 |
| Fractal patch length scale 2 | $K_{L_b}$    | 0.20 ~ 0.33 |
| Fractal patch width scale 1  | $K_{W_a}$    | 0.10 ~ 0.33 |
| Fractal patch width scale 2  | $K_{W_b}$    | 0.20 ~ 0.33 |

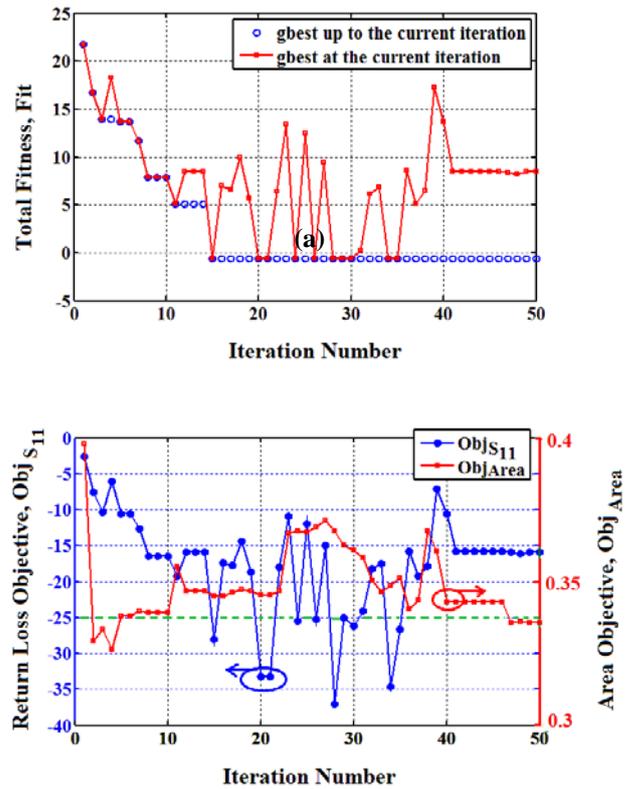
The number of particles used here is 32, i.e., 4 particles for each of the eight geometrical parameter. Furthermore, a stop criterion is chosen such that 50 PSO iterations are reached or the fitness function remains unchanged with less than 2% error for at least 20 successive iterations.

#### 4. RESULTS AND DISCUSSION

Illustrative results related to the design of a third-order Minkowski fractal antenna are given here. The threshold value of  $S_{11}$ ,  $(S_{11})_{th}$ , used in the fitness

function is  $-25 \text{ dB}$ . Figure 4 reveals that the progress of the PSO algorithm as a function of iteration number. Return loss and area objective functions as well total fitness function is illustrated in this figure.

The PSO algorithm creates an optimal miniaturized patch antenna size. Table 3 summarizes the final optimized geometrical parameters.



**Fig 4:** Variation of objective function with PSO iteration number for MFA3 (a) total (b) return loss and area.

**Table 3:** Optimized geometrical parameters of MFA3.

| Parameter    | Value |
|--------------|-------|
| $K_{L_p}$    | 0.426 |
| $K_{L_s}$    | 1.060 |
| $K_{W_s}$    | 0.190 |
| $K_{L_{st}}$ | 0.208 |
| $K_{L_a}$    | 0.169 |
| $K_{L_b}$    | 0.258 |
| $K_{W_a}$    | 0.247 |
| $K_{W_b}$    | 0.276 |

The performance results of the optimized MFA3 are carried out from the electromagnetic simulator CST. Table 4 lists some of the simulation results, namely, return

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loss  $S_{11}$ , antenna gain  $G$ , total antenna efficiency  $\eta$ , bandwidth  $BW$ , and patch size reduction  $\Delta A_p$ . The size Reduction is computed as

$$\Delta A_p = \frac{A_F - A_R}{A_R} \quad (11)$$

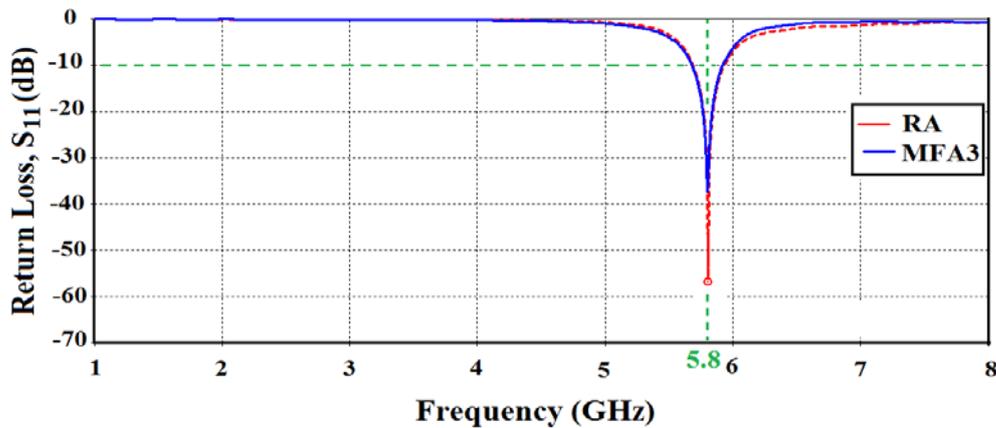
**Table 4:** Simulation results of optimized MFA3 and RA.

| Antenna Performance Parameters | Antenna Type |        |
|--------------------------------|--------------|--------|
|                                | RA           | MFA3   |
| $S_{11}$ (dB)                  | -56.96       | -37.37 |
| $G$ (dB)                       | 6.08         | 4.48   |
| $\eta$ (%)                     | 96.25        | 96.25  |
| $BW$ (GHz)                     | 0.24         | 0.24   |
| $f_L$ (GHz)                    | 5.696        | 5.68   |
| $f_H$ (GHz)                    | 5.93         | 5.92   |
| $A_p$ (mm <sup>2</sup> )       | 210.35       | 72.55  |
| $\Delta A_p$ (%)               | -            | 65.51  |

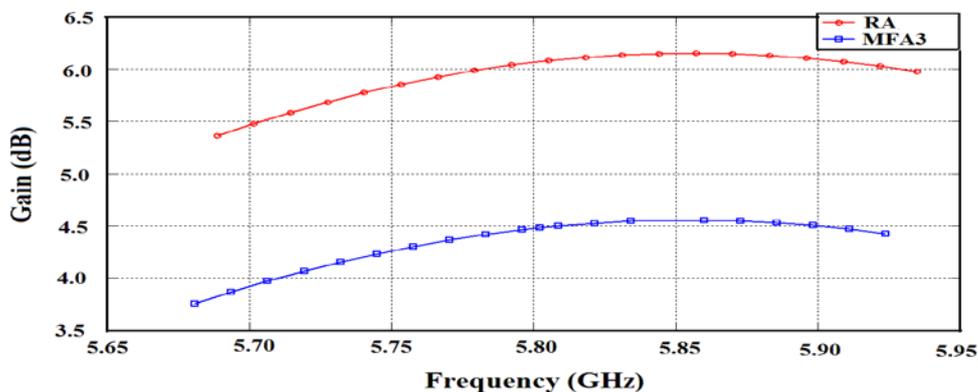
Investigating the results in Table 4 reveals that

- The area of the optimized fractal patch antenna is equal to 34.5% of the area of the reference antenna.
- A return loss less than  $-37$  dB, gain greater than  $4.4$  dB, and efficiency greater than 96% are obtained from RA and MFA3
- Both RA and MFA3 have the same bandwidth (240 MHz at  $-10$  dB). Also, the lower and upper frequencies are nearly the same for the two antennas.

The return losses of optimized MFA3 together with reference counterpart are illustrated in Fig. 5. The two curves are almost the same over the whole frequency regions. Figures 6a and 6b show, respectively, the gain and efficiency for the designed antennas. It is clear from these figures that the 3rd-order fractal has almost similar spectral behavior.

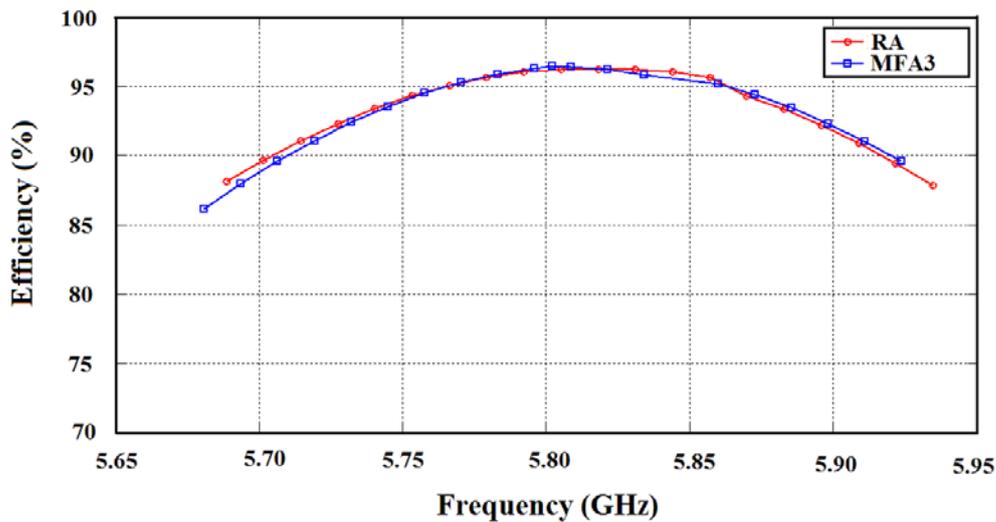


**Fig 5:** Simulated return losses of the optimized antenna. Results related to the reference antenna are given for comparison purposes.



(a)

**Fig 6:** Gain (a) and efficiency (b) of the optimized fractal antenna. Results related to the reference antenna are also given.



(b)

Fig 6: (Continued.)

The surface current distributions of RA and MFA3 antenna are displayed in Fig. 7. One can depict from this figure that the radiation is achieved from the vertical (width) side of the two antennas since the currents induced in the two vertical sides are of the same amplitude and direction. The radiation from horizontal (length) side is less from the vertical side because the currents in the two horizontal sides are of opposite direction and having different amplitudes. Thus, the width side has more effect on radiation than the length side. In other words, the width of patch antenna represents radiation side while the length of patch antenna represents resonance side.

The 3D radiation patterns of the two antennas are displayed in Fig. 8. It's shown that radiation patterns of the two antennas are almost the same. Figure 9 shows the radiation pattern in the elevation direction  $yz$  ( $\theta = 90^\circ$ ) and  $xy$  ( $\theta = 90^\circ$ ) planes and azimuth direction  $xz$  ( $\theta = 0^\circ$ ) plane at  $5.8 \text{ GHz}$  for the antennas. It is appears that the fractal antenna radiates nearly omni directionally. The radiation patterns show two nulls for  $E_\theta$  component at  $\theta = 0^\circ$  and  $\theta = 180^\circ$  for  $xz$ - and  $xy$ -plane, respectively, and two nulls for  $E_\phi$  component at  $\phi = 90^\circ$  and  $\phi = -90^\circ$  for  $xz$ - and  $xy$ - planes, respectively.

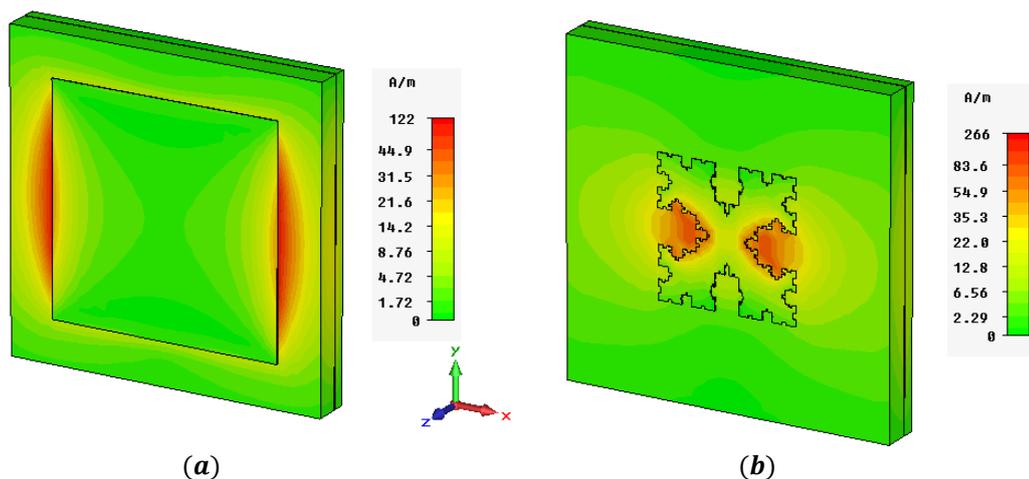


Fig 7: Current distribution on antenna surface; (a) RA (b) MFA3.

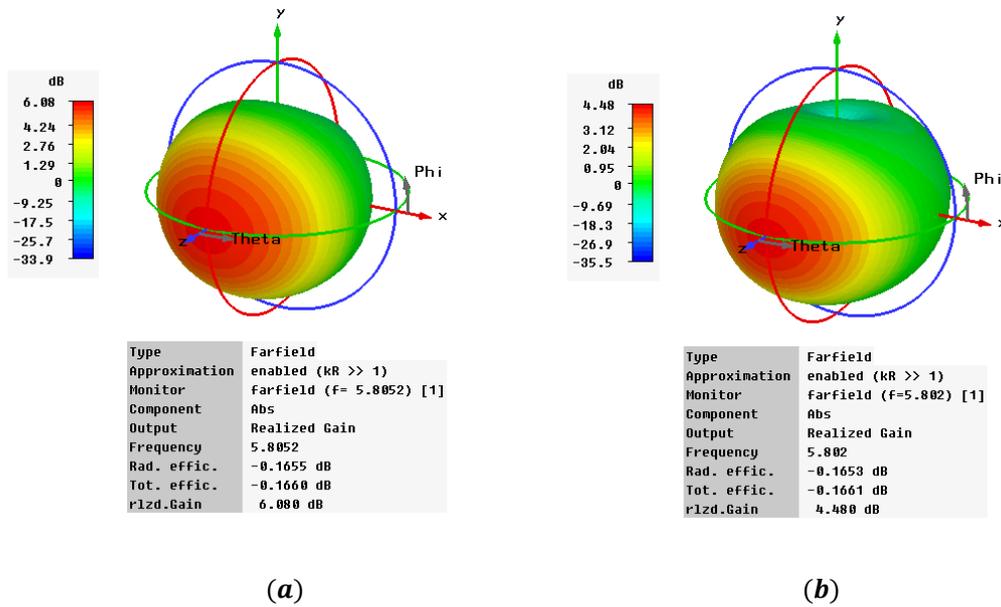


Fig 8: 3D Radiation patterns for the Minkowski fractal aperture antenna; (a) RA (b) MFA3.

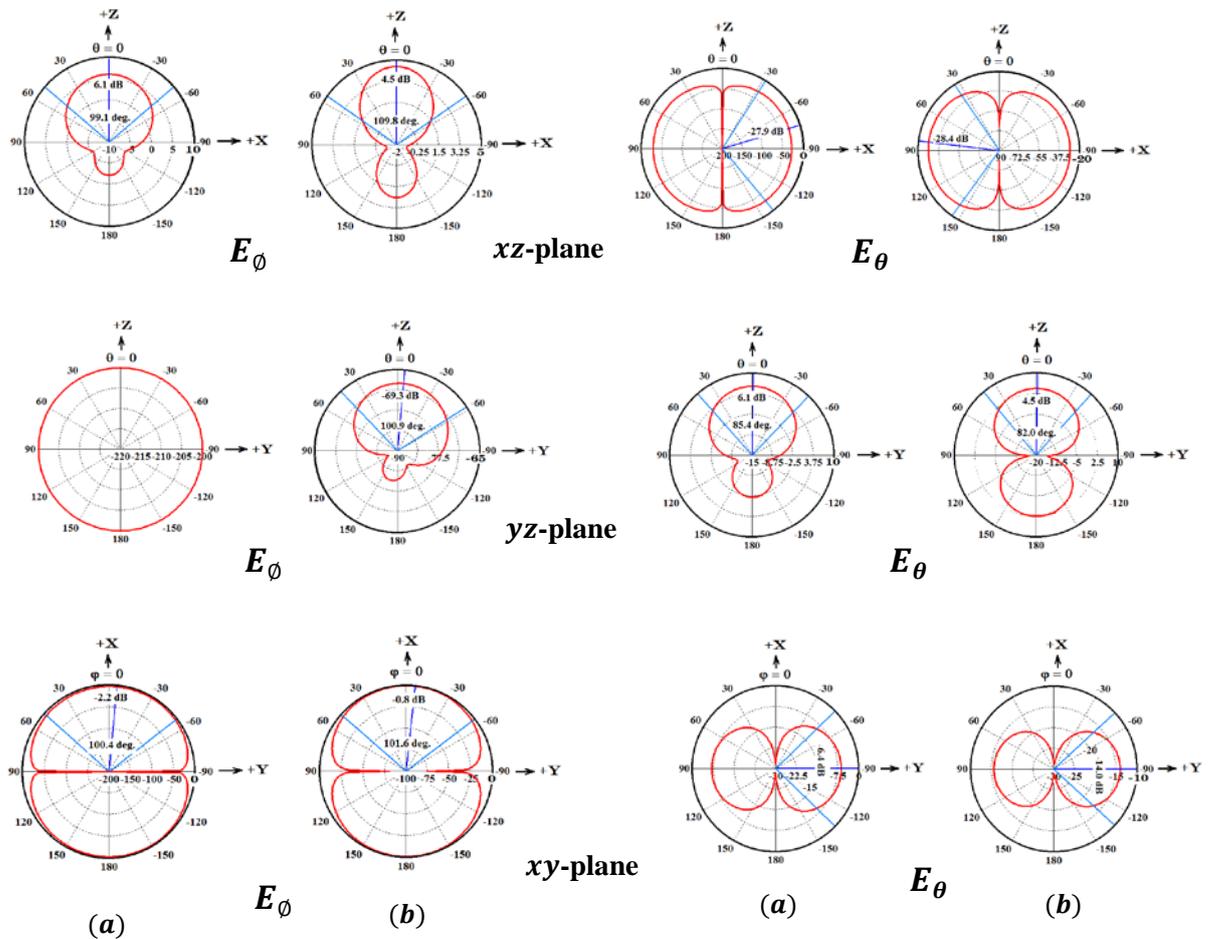


Fig 9: Radiation patterns for the Minkowski fractal aperture antenna; (a) RA (b) MFA3.

## 5. CONCLUSION

A miniaturized Minkowski fractal aperture-coupled antenna for 5.8 GHz RFID applications has been designed and investigated. The antenna geometrical parameters are optimized using PSO algorithm which runs on MATLAB environments and synchronously coupled to full wave electromagnetic simulator implemented using CST Microwave Studio software. The used optimization objective functions reflect both return loss and antenna size. The results reveals that more than 65% reduction in patch antenna size with fixed ground plane can be obtained as compared with the conventional reference antenna. Further, excellent performance requirements have been obtained with less than  $-37$  dB return loss and more than 4 dB gain associated stable radiation pattern.

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